

Simultaneous Equations

Created by:

www.pinpointlearning.co.uk

The Personalised GCSE Revision Site

1) Simultaneous Equations: Easier

1) Solve the simultaneous equations.

① $2x + 3y = 9$

② $5x + 3y = 18$

② - ①

$$5x + 3y = 18$$

$$2x + 3y = 9 \quad -$$

$$\frac{3x}{3} = \frac{9}{3}$$

$$x = 3$$

Sub $x = 3$ into ①

$$2x + 3y = 9$$

↓

$$6 + 3y = 9$$

$$3y = 3$$

$$y = 1$$

$$x = \underline{\quad 3 \quad}$$

$$y = \underline{\quad 1 \quad}$$

(3 Marks)

2) Solve the simultaneous equations.

① $4x + 2y = 9 \quad \times 2$

② $8x + 8y = 20$

③ $8x + 4y = 18$

Sub $y = 0.5$ into ①

$$4x + 1 = 9$$

$$\frac{4x}{4} = \frac{8}{4}$$

$$x = 2$$

$$x = \underline{\quad 2 \quad}$$

$$y = \underline{\quad 0.5 \quad}$$

(4 Marks)

1) Simultaneous Equations: Medium

7) Solve the simultaneous equations.

$$\textcircled{1} \quad 6x + 3y = 15 \quad \times 3$$

$$\textcircled{2} \quad 4x - 9y = -34$$

$$\textcircled{3} \quad 18x + 9y = 45$$

$\textcircled{2} + \textcircled{3}$

$$\begin{array}{r} 4x - 9y = -34 \\ 18x + 9y = 45 \\ \hline 22x = 11 \\ \hline 22 \quad x = 0.5 \end{array}$$

Sub $x = 0.5$ into $\textcircled{1}$

$$\begin{array}{r} 3 + 3y = 15 \\ -3 \quad -3 \\ \hline 3y = 12 \\ \hline 3 \quad y = 4 \end{array}$$

$$\begin{array}{l} x = 0.5 \\ y = 4 \end{array}$$

(4 Marks)

8) Solve the simultaneous equations.

$$\textcircled{1} \quad 5x + 2y = 29 \quad \times 3$$

$$\textcircled{2} \quad 8x - 6y = 51$$

$$\textcircled{3} \quad 15x + 6y = 87$$

$\textcircled{2} + \textcircled{3}$

$$\begin{array}{r} 8x - 6y = 51 \\ 15x + 6y = 87 \\ \hline 23x = 138 \\ \hline 23 \quad x = 6 \end{array}$$

Sub $x = 6$ into $\textcircled{1}$

$$\begin{array}{r} 30 + 2y = 29 \\ -30 \quad -30 \\ \hline 2y = -1 \\ \hline 2 \quad y = -0.5 \end{array}$$

$$\begin{array}{l} x = 6 \\ y = -0.5 \end{array}$$

(4 Marks)

1) Simultaneous Equations: Harder

9) Bill goes into a chip shop and buys **3 fish** and **2 portions of chips**, it cost him £5.20

Jenny also goes into the same chip shop. She buys **5 fish** and **6 portions of chips**, it cost her £10.80

What is the cost of a portion of fish and chips?

$$\begin{array}{l}
 \textcircled{1} \quad 3f + 2p = 5.20 \quad \times 3 \\
 \textcircled{2} \quad 5f + 6p = 10.80 \\
 \textcircled{3} \quad 9f + 6p = 15.60 \\
 \textcircled{3} - \textcircled{2} \\
 \hline
 4f = 4.80 \\
 f = 1.20
 \end{array}$$

Sub into ①

$$\begin{array}{r}
 3.60 + 2p = 5.20 \\
 -3.60 \quad -3.60 \\
 \hline
 2p = 1.60 \\
 p = 0.80
 \end{array}$$

$f + p = \pounds 2$

(5 Marks)

10) There are some ducks and some sheep on a farm. Altogether they have 35 heads and 94 feet.

How many ducks and sheep are there?

$$\begin{array}{l}
 \textcircled{1} \quad d + s = 35 \text{ (heads)} \quad \times 2 \\
 \textcircled{2} \quad 2d + 4s = 94 \text{ (feet)} \\
 \textcircled{3} \quad 2d + 2s = 70 \\
 \textcircled{2} - \textcircled{3} \\
 \hline
 2s = 24 \\
 s = 12
 \end{array}$$

Sub $s = 12$ into ①

$$\begin{array}{r}
 d + 12 = 35 \\
 -12 \quad -12 \\
 \hline
 d = 23
 \end{array}$$

Ducks = 23
Sheep = 12

(5 Marks)